

#### Year 5 | Summer Term | Week 1 to 4 – Number: Decimals



# Overview Small Steps

#### Adding decimals within 1

- Subtracting decimals within 1
- Complements to 1
- Adding decimals crossing the whole
- Adding decimals with the same number of decimal places
- Subtracting decimals with the same number of decimal places
- Adding decimals with a different number of decimal places
- Subtracting decimals with a different number of decimal places
  - Adding and subtracting wholes and decimals
- Decimal sequences
- Multiplying decimals by 10, 100 and 1,000
- Dividing decimals by 10, 100 and 1,000

### **NC** Objectives

Recognise and write decimal equivalents of any number of tenths or hundredths.

Find the effect of dividing a one or two digit number by 10 or 100, identifying the value of the digits in the answer as ones, tenths and hundredths

Solve simple measure and money problems involving fractions and decimals to two decimal places.

Convert between different units of measure [for example, kilometre to metre]



### Adding Decimals within 1

#### Notes and Guidance

Children add decimals within one whole. They use place value counters and place value charts to support adding decimals and understand what happens when we exchange between columns.

Children build on their understanding that 0.45 is 45 hundredths, children can use a hundred square to add decimals.

### Mathematical Talk

What is the number represented on the place value chart? What digit changes when I add a hundredth?

How many hundredths can I add before the tenths place changes? Explain why.

How can the children shade in the hundred square to support their calculations?

Why does using column addition support adding decimals? What is the same and what is different?

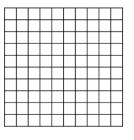
# Varied Fluency

Use this place value chart to help answer the questions.

| Ones | Tenths | Hundredths | Thousandths |  |
|------|--------|------------|-------------|--|
|      | 01 01  | 0.01       | 0.001       |  |

- What number is one hundredth more?
- Add 0.3, what number do you have now?
- How many more thousandths can I add before the hundredths digit changes?

Each box in this hundred square represents one hundredth of the whole. Use this to answer:



Use the column method to complete the additions.

0.45 + 0.5

3

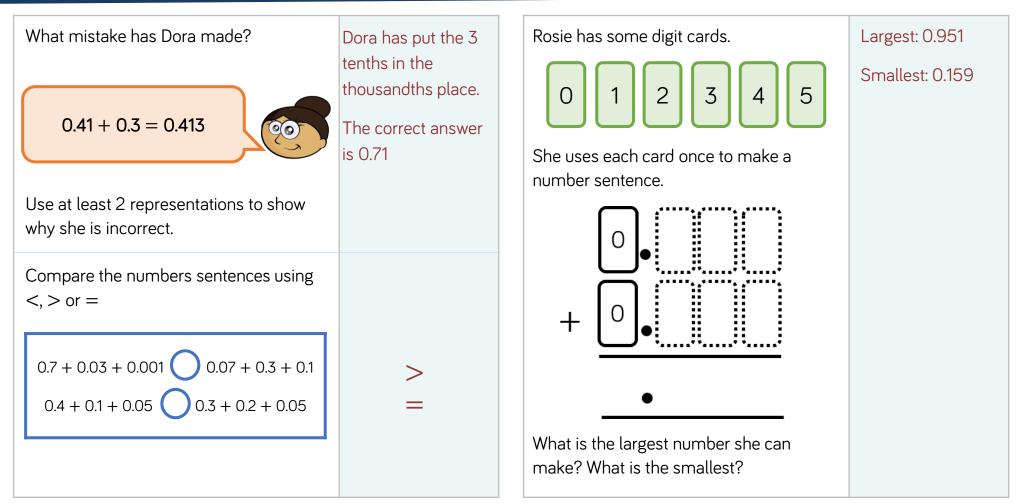
0.45 + 0.05





### Adding Decimals within 1

### **Reasoning and Problem Solving**





### Subtracting Decimals within 1

### Notes and Guidance

Children subtract decimals using a variety of different methods.

They look at subtracting using place value counters on a place value grid. Children also explore subtraction as difference by using a number line to count on from the smaller decimal to the larger decimal.

Children use their knowledge of exchange within whole numbers to subtract decimals efficiently.

### Mathematical Talk

What is the number represented on the place value chart?

What is one tenth less than one?

What is one hundredth less than one?

Show me how you know.

If I'm taking away tenths, which digit will be affected? Is this always the case?

How many hundredths can I take away before the tenths place is affected?

# Varied Fluency

Here is a number.

| Ones | Tenths | Hundredths | Thousandths            |  |  |
|------|--------|------------|------------------------|--|--|
|      | 3      | 555        | 0001 0001<br>0001 0001 |  |  |

- What is three tenths less than the number?
- Take away 0.02, what is your number now?
- Subtract 5 thousandths. What is the final number?

Find the difference between the two numbers using the number line.

 $\begin{array}{c} 0.424 & 0.618 \\ \\ \text{Calculate.} \\ \hline 0.584 - 0.154 = & 0.44 - 0.1 = \\ 0.684 - 0.254 = & 0.44 - 0.09 = \\ 0.685 - 0.255 = & 0.44 - 0.11 = \end{array}$ 

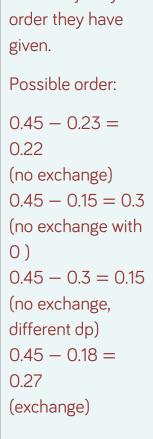


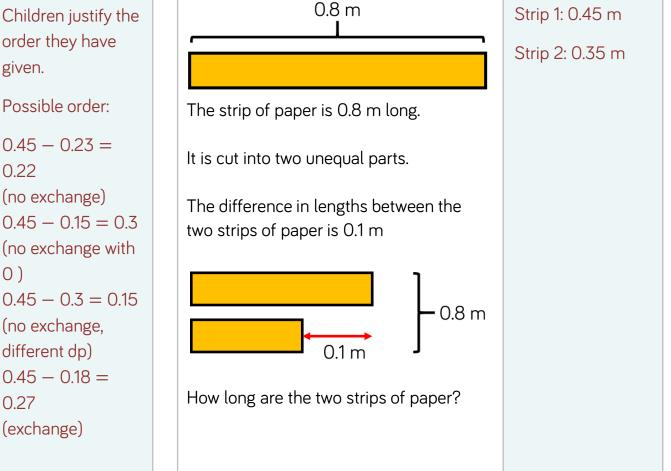
### Subtracting Decimals within 1

### **Reasoning and Problem Solving**

Here are four calculations. Which one is the easiest to answer? Which one is the trickiest to answer? Explain your choice of order.

0.45 - 0.3 =0.45 - 0.15 =0.45 - 0.23 =0.45 - 0.18 =







### Complements to 1

### Notes and Guidance

Children find the complements which sum to make 1

It is important for children to see the links with number bonds to 10, 100 and 1000

This will support them when finding complements to 1, up to three decimal places.

Children can use a hundred square, part-whole models and number lines to support finding complements to one.

### Mathematical Talk

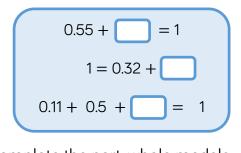
What number bonds can you use to help you?

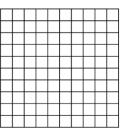
- How can shading the hundred square help you find the complement to 1?
- How many different ways can you make 1? How many ways do you think there are?

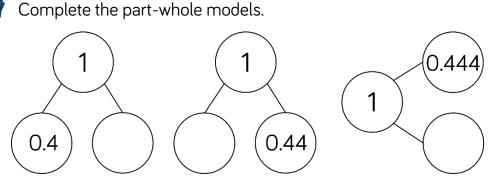
If I add \_\_\_\_\_, which place will change? How many can I add to change the tenths/hundredths place?

### Varied Fluency

Using a blank hundred square, where each square represents one hundredth, find the complements to 1 for these numbers.







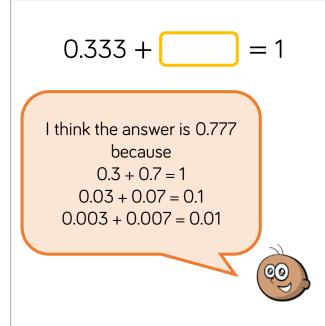
Use the number line to find the complements to 1





#### Complements to 1

### Reasoning and Problem Solving



Do you agree with Tommy? Can you explain what his mistake was? Tommy has forgotten that when you have ten in a place value column you need to use your rules of exchanging.

```
e.g.
10 tenths = 1 one
10 hundredths =
1 tenth
10 thousandths =
1 hundredth
```

The correct answer is 0.667 How many different ways can you find a path through the maze, adding each number at a time, to make a total of one?

| Start → | 0.02  | 0.01  | 0.05  | 0.08 | 0.3   | 0.04  | 0     | 0.001 |
|---------|-------|-------|-------|------|-------|-------|-------|-------|
|         | 0.2   | 0.06  | 0.07  | 0.09 | 0.001 | 0.004 | 0.02  | 0.04  |
|         | 0.005 | 0.04  | 0.2   | 0.02 | 0.05  | 0.06  | 0.07  | 0.6   |
|         | 0.5   | 0.005 | 0.05  | 0.02 | 0.03  | 0.017 | 0.006 | 0.06  |
|         | 0.009 | 0.8   | 0.001 | 0.05 | 0.015 | 0.01  | 0.008 | 0.007 |
|         | 0.09  | 0.2   | 0.08  | 0.03 | 0.199 | 0.01  | 0.04  | 0.05  |
|         | 0.01  | 0.008 | 0.1   | 0.09 | 0.005 | 0.08  | 0.02  | 0.02  |
|         | 0.05  | 0.03  | 0.01  | 0.22 | 0.07  | 0.003 | 0.04  | 0.09  |

| 0.02  | 0.01  | 0.05  | 0.08 | 0.3   | 0.04  | 0     | 0.001 |
|-------|-------|-------|------|-------|-------|-------|-------|
| 0.2   | 0.06  | 0.07  | 0.09 | 0.001 | 0.004 | 0.02  | 0.04  |
| 0.005 | 0.04  | 0.2   | 0.02 | 0.05  | 0.06  | 0.07  | 0.6   |
| 0.5   | 0.005 | 0.05  | 0.02 | 0.03  | 0.017 | 0.006 | 0.06  |
| 0.009 | 0.8   | 0.001 | 0.05 | 0.015 | 0.01  | 0.008 | 0.007 |
| 0.09  | 0.2   | 0.08  | 0.03 | 0.199 | 0.01  | 0.04  | 0.05  |
| 0.01  | 0.008 | 0.1   | 0.09 | 0.005 | 0.08  | 0.02  | 0.02  |
| 0.05  | 0.03  | 0.01  | 0.22 | 0.07  | 0.003 | 0.04  | 0.09  |

→ 1

Once you have found a way, can you design your own smaller maze for others to solve?



# Adding - Crossing the Whole

#### Notes and Guidance

Children use their skills at finding complements to 1 to support their thinking when crossing the whole. Children require flexibility at partitioning decimals, as bridging will be extremely important. Encourage children to make one first, then add the remaining decimal.

For example: 0.74 + 0.48 =

0.74 + 0.26 + 0.22 = 1.22

### Mathematical Talk

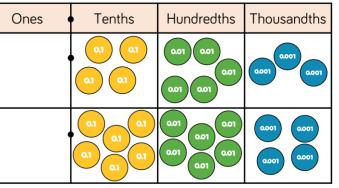
What happens when we have 10 in a place value column?

How would partitioning a number help us? How do you decide what number to partition? Why is partitioning 0.67 into 0.55 and 0.12 more helpful than 0.6 and 0.07?

What complement to 1 would I use to answer this question?

# Varied Fluency

Use the place value grid to answer 0.453 + 0.664

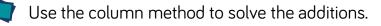


Amir is using complements to 1 to add decimals.

Use Amir's method to solve: a) 0.56 + 0.78 b) 3.42 + 0.79

0.92 + 0.8

0.45 + 0.55 + 0.12 = 1.12

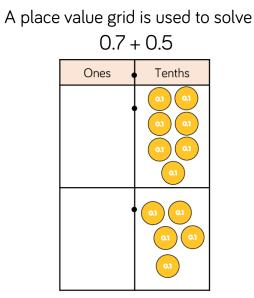






### Adding – Crossing the Whole

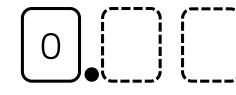
### **Reasoning and Problem Solving**



Alex thinks the answer is 0.12 What mistake has she made? Ten lots of one tenth is one whole. There are 12 tenths so Alex needs to make an exchange. She should exchange 10 tenths for 1 one.

The correct answer is 1.2

You will need a partner and a six-sided dice for this game.



Take it in turns rolling the dice twice and placing the digits in the blank spaces above. Record the number in a table.

Swap over with your partner.

Roll the dice again and add your new number to the first number. The winner is the person who after adding 4 numbers is the closest to 1.5 **without** going over. Example:

Player 1 rolls a 1 and a 4. 0.14

Player 1 then rolls a 2 and a 6. 0.26

0.14 + 0.26 = 0.38

| Player 1 | Player 2        |
|----------|-----------------|
| 0.14     | 0.64            |
| 0.38     | 1.23            |
| 0.69     | 1.49            |
| 1.24     | <del>1.60</del> |



4 5

### Adding – Same Decimal Places

### Notes and Guidance

Children add numbers greater than one with the same number of decimal places.

Place value grids and counters are extremely helpful in ensuring children are understanding the value of each digit and understanding when to exchange.

Ensure children see the formal written method (column addition) alongside the place value chart.

### Mathematical Talk

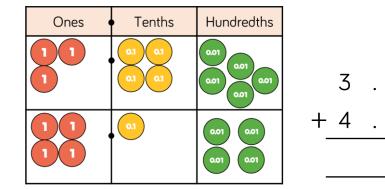
Why is it important to line up the columns?

What happens when there are a total of ten counters in a place value column?

Why is the position of the decimal point important?

### Varied Fluency

Use the place value chart to add 3.45 and 4.14



Use the column method to solve these additions.

| Z   | 4. | 4 | 2 |  |   | 4 | • | 5 | 5 |
|-----|----|---|---|--|---|---|---|---|---|
| + 7 | 7. | 6 | 3 |  | + | 3 | • | 0 | 7 |

Ron goes to the shops. He buys 3 items. What is the most he could pay? What is the least he could pay?

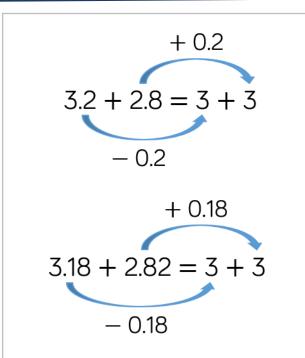


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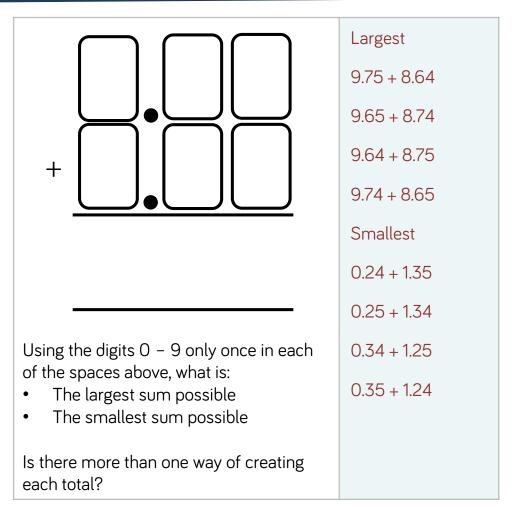
### Adding – Same Decimal Places

### **Reasoning and Problem Solving**



Using these strategies, can you find more number sentences which have the same total as 3 + 3

Children may find a range of answers. The important teaching point is to highlight that you have added the same to one number as you have taken away from the other.





### Subtract – Same Decimal Places

### Notes and Guidance

Children subtract numbers with the same number of decimal places. They use place value counters and a place value grid to support them with exchanging.

Children should be given opportunities to apply subtraction to real life contexts which could involve measures. Bar models can be a useful representation of the problems.

### Mathematical Talk

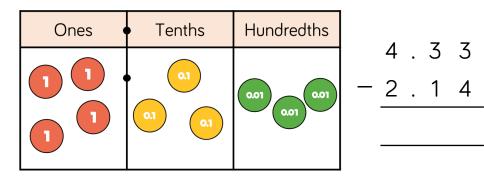
What happens when you need to subtract a greater digit from a smaller digit e.g. 3 hundredths subtract 4 hundredths?

How many tenths are equivalent to one hundredth?

- Do we only ever make one exchange in a subtraction calculation?
- Which of these numbers will need exchanging?
- Can you predict what the answer might be?
- How could you check your answer?

### Varied Fluency

Use the place value chart to find the to answer 4.33 - 2.14



Use the column method to answer these questions.

| 6.4  | 5.05      |
|------|-----------|
| -3.8 | - 2 . 1 5 |

Jack has £12.54 in his wallet. He buys a football which costs £5.82



How much money does he have left?

Annie has £4.50



### Subtract – Same Decimal Places

### **Reasoning and Problem Solving**

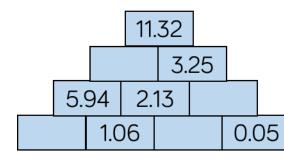
Dexter and Annie have some money. Dexter has  $\pounds 3.45$  more than Annie.

They have £12.45 altogether.

How much money does Annie have?

| Dexter |  |
|--------|--|
| Annie  |  |

In this number pyramid, each number is calculated by adding the two numbers underneath.



|     |     |       | 11. | 32             |    |     |    |
|-----|-----|-------|-----|----------------|----|-----|----|
| _   |     | 8.    | 07  | 3.             | 25 |     |    |
|     | 5.9 | 94 2. |     | 13 <b>1</b> .′ |    | 12  |    |
| 4.8 | 8   | 1.06  |     | 1.07           |    | 0.0 | 05 |



### Adding – Different D.P.

#### Notes and Guidance

Children add numbers with different numbers of decimal places. They focus on the importance of lining up the decimal point in order to ensure correct place value.

Children should be encouraged to think about whether their answers are sensible. For example, when adding 1.3 to 1.32 and getting an answer 1.45, how do we know it is not a sensible answer? Discuss the importance of estimation.

### Mathematical Talk

Why is the decimal point important when we are reading and writing a number?

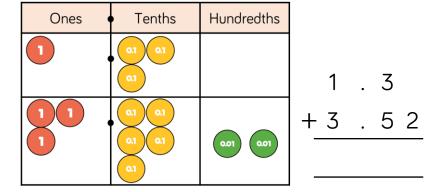
What would a sensible estimate be?

Is this a sensible answer? Why/why not?

What advice would you give to someone that is struggling with recording their numbers in the correct place?

### Varied Fluency

Use the place value grid to add 1.3 and 3.52



Use the column method to answer these questions.

| 4   | . 4     | 4.    | 42 |
|-----|---------|-------|----|
| + 7 | . 0 4 4 | + 1 . | 6  |

Whitney is cycling in a race.

She has cycled 3.145 km so far and has 4.1 km left to go. What is the total distance of the race?

15



### Adding – Different D.P.

### **Reasoning and Problem Solving**

Eva is trying to find the answer to

4.144 + 1.4

Here is her working out.

| $\bigcap$ | 4 | • | 1 | 4 | 4 |  |
|-----------|---|---|---|---|---|--|
| +         |   |   | 1 | • | 4 |  |
|           | 4 | • | 2 | 4 | 8 |  |
|           |   |   |   |   |   |  |

Can you spot and explain her error?

Work out the correct answer.

The digits are lined up incorrectly.

Eva needs to line up the decimal point.

The correct answer is 5.544

|             | e calcula                         | No exchange:                             |  |   |                                |
|-------------|-----------------------------------|--|--|---|--------------------------------|
| column      | in the tat                        | ole.                                     |  |   | 9.99 + 0.001                   |
| 9.9         | 9 + 0.                            | 1  | 9.99 -                                     | ⊦ 1   | Exchange in the ones column:   |
| 9.99        | + 0.0                             | 01                                       | 9.99 +                                     | 0.01  | 9.99 + 1                       |
| Some ca     | alculatior                        | ns might                                 | need to                                    | go in                                       | 9.99 + 0.1                     |
| more tha    | an one p                          | lace.                                    |  |   | 9.99 + 0.01                    |
| No exchange | Exchange in<br>the ones<br>column | Exchange in<br>the tenths<br>column      | Exchange in<br>the<br>hundredths<br>column | Exchange in<br>the<br>thousandths<br>column | Exchange in the tenths column: |
|             |                                   |  |  |   | 9.99 + 0.1                     |
|             |                                   |  |  |   | 9.99 + 0.01                    |
| Add 2 m     | nore calc                         | Exchange in the<br>hundredths<br>column: |  |   |                                |
|             |                                   | 9.99 + 0.01                              |  |   |                                |



### Subtracting – Different D.P.

### Notes and Guidance

Children subtract decimals with different numbers of decimal places.

They continue to focus on the importance of lining up the decimal point in order to ensure correct place value.

Children identify the importance of zero as a place holder.

### Mathematical Talk

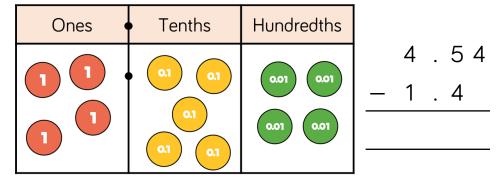
What does it mean if there is nothing in a place value column? How can we represent this in the formal written method?

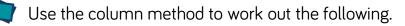
What do you notice about 4.7 - 3.825 and 4.699 - 3.824? Is one of them more difficult than the other? Why?

Are there more efficient methods for this question?

### Varied Fluency

Use the place value grid to help subtract 1.4 from 4.54





How much change would I get from £10 if I bought a bag of apples costing £4.27?





### Subtracting – Different D.P.

### **Reasoning and Problem Solving**



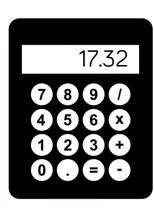
If there are 5 hundredths and I subtract nothing from it then there are still 5 hundredths.

|   | 4 | • | 9 |   |
|---|---|---|---|---|
| _ | 3 | • | 8 | 5 |
|   | 1 |   | 1 | 5 |

Do you agree with Whitney? Explain your answer. Whitney is not correct. She needs to use zero as a place value holder in the hundredths column of 4.9 and then exchange.

Encourage children to explore more efficient mental strategies as well as correcting the formal method.

The correct answer is 1.05



Teddy used a calculator to solve: 31.4 - 1.408

When he looked at his answer of 17.32 he realised he'd made a mistake.

He had typed all the correct digits in.

Can you spot his mistake? What should the correct answer be? Teddy placed the decimal point after the 4 making 14.08 instead of 1.408

The correct answer is 29.992



#### Wholes and Decimals

### Notes and Guidance

Children add and subtract numbers with decimals from whole numbers. Highlight that whole numbers are written without a decimal point.

There may be a misconception when recording integers, link this to the place value grid. Emphasise prior understanding that the decimal point is to the right of the ones place.

### Mathematical Talk

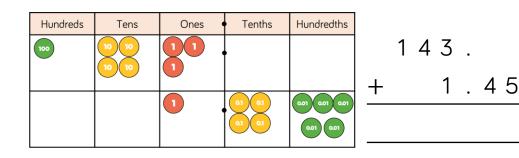
What is a whole number/integer?

- Where can we add a decimal point to the number 143 so that its value stays the same?
- What's the same and what's different about 10 and 10.0?
- Can you use different methods? (Number line, column subtraction, mentally).

Which is most efficient for this calculation? Explain why.

## Varied Fluency

Use the place value grid to help add 143 and 1.45



| ι 1 | Use the place value grid to help work out $12 - 1.2$ |            |            |             |                    |     |  |  |  |  |
|-----|--|------------|------------|-------------|--------------------|-----|--|--|--|--|
|     |  | Tens       | Ones       | Tenths      |                    | 12. |  |  |  |  |
|     |  | 10         |            | •           |                    | 1.2 |  |  |  |  |
| F   | ind t  | he most ef | ficient me | thod to sol | ve this calculatio | ns. |  |  |  |  |
|     |  | 43 — 2.1   | 4 + 0.86 : | =           | 19 – 0.25 =        |     |  |  |  |  |

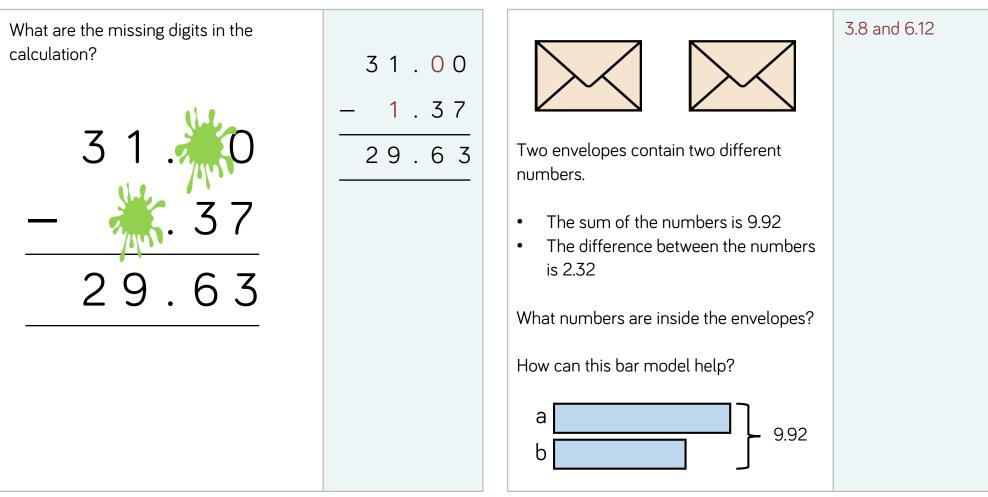
23 + 4.105 =

19 — 17.37 =



#### Wholes and Decimals

### **Reasoning and Problem Solving**





### **Decimal Sequences**

#### Notes and Guidance

Children look at decimal sequences and create simple rules, for example: adding 0.5 every time.

It is important to note that they are not expected to generate algebraic expressions for the sequences, but the use of the word 'term' could be used to predict the next number in the sequence. For example, what would be the value of the 10th term in the sequence?

### Mathematical Talk

What do increasing and decreasing mean?

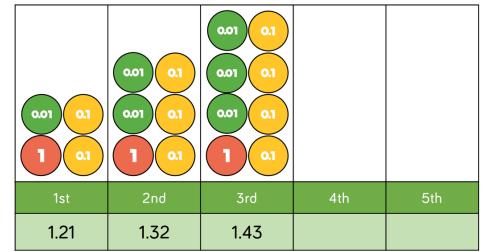
Is the sequence increasing by the same amount each time? By how much?

What is the same about each term? What is changing in each term?

What will the next term in the sequence be?

### Varied Fluency

#### Complete the sequence.



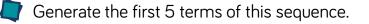
#### Write the rules for each sequence.

0.45, 0.6, 0.75, 0.9

The rule is

1.25, 2.5, 3.75, 5, 6.25

The rule is

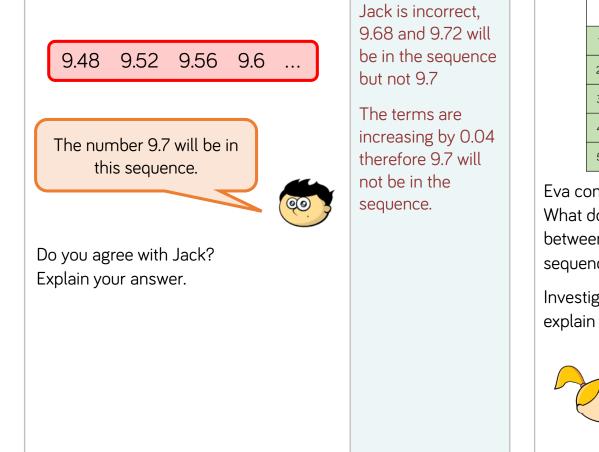


The 1<sup>st</sup> term is 1.74 The sequence decreases by 0.24 each time.



### **Decimal Sequences**

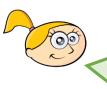
### Reasoning and Problem Solving



|                      | 1 <sup>st</sup> | Relationship | 2 <sup>nd</sup> |
|----------------------|-----------------|--------------|-----------------|
|                      | sequence        |              | sequence        |
| 1 <sup>st</sup> term | 0.1             |              | 1               |
| 2 <sup>nd</sup> term | 0.2             |              | 2               |
| 3 <sup>rd</sup> term | 0.3             |              | 3               |
| 4 <sup>th</sup> term | 0.4             |              | 4               |
| 5 <sup>th</sup> term |                 |              |                 |

Eva compared the two sequences above. What do you notice about the differences between the terms in the two sequences?

Investigate Eva's sequences below and explain your thinking.



I wonder what the differences would be between sequences that go up in + 0.01 and +1 sequence...

#### The difference between the terms is increasing by 0.9 each time e.g. $1^{st} + 0.9$ $2^{nd} + 1.8$ $3^{rd} + 2.7$ $4^{th} + 3.6$

Children may also notice that the terms in the 2<sup>nd</sup> sequence are ten times larger than in the first.

The differences would increase by 0.99 each time.



# Multiply by 10, 100 and 1,000

### Notes and Guidance

Children learn how to multiply numbers with decimals by 10, 100 and 1,000 They look at moving the counters in a place value grid to the left in order to multiply by multiples of 10 Children may have previously made the generalisation that when a number is ten times greater they put a zero on the end of the original number. This small step highlights the importance of understanding the effect of multiplying both integers and decimal numbers by multiples of 10.

### Mathematical Talk

What is the value of each digit? Where would these digits move to if I multiplied the number by 10?

Why is the zero important in this number? Could we just take it out to make it easier for ourselves? Why/why not?

What do you notice about the numbers you are multiplying in the table?

# Varied Fluency

Use the place value grid to multiply 3.24 by 10, 100 and 1,000

| Thousands | Hundreds | Tens | Ones | Tenths | Hundredths |
|-----------|----------|------|------|--------|------------|
|           |          |      | •••• | •      | 0          |

When you multiply by \_\_\_\_\_, you move the counters \_\_\_\_\_ places to the left.

2.401

Use a place value grid to multiply these decimals by 10, 100 and 1,000

4.24



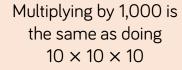
Complete the table below.

|       | ×10 | ×100 | ×1,000 |
|-------|-----|------|--------|
| 3.14  |     |      |        |
| 13    |     |      |        |
| 0.233 |     |      |        |



### Multiply by 10, 100 and 1,000

### **Reasoning and Problem Solving**





you move the

the left in both

cases.

Do you agree with Mo? Explain your answer.

Mo is correct, as Using the digits 0-9 create a number with up to 3 decimal places, for example, digits 3 places to 3.451

> Cover the number using counters on your Gattegno chart.

| 10,000 | 20,000 | 30,000 | 40,000 | 50,000 | 60,000 | 70,000 | 80,000 | 90,000 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1,000  | 2,000  | 3,000  | 4,000  | 5,000  | 6,000  | 7,000  | 8,000  | 9,000  |
| 100    | 200    | 300    | 400    | 500    | 600    | 700    | 800    | 900    |
| 10     | 20     | 30     | 40     | 50     | 60     | 70     | 80     | 90     |
| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      |
| 0.1    | 0.2    | 0.3    | 0.4    | 0.5    | 0.6    | 0.7    | 0.8    | 0.9    |
| 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
| 0.001  | 0.002  | 0.003  | 0.004  | 0.005  | 0.006  | 0.007  | 0.008  | 0.009  |

Explore what happens when you multiply your number by 10, then 100, then 1,000 What patterns do you notice?

Children will be able to see how the counter will move up a row for multiplying by 10, two rows for 100 and three rows for 1,000. They can see that this happens to each digit regardless of the value.

For example,

 $3.451 \times 10$ becomes 34.51

Each counter moves up a row but stays in the same column.



# Divide by 10, 100 and 1,000

### Notes and Guidance

Children learn how to divide numbers with decimals by 10, 100 and 1,000

Children use the place value chart to support the understanding of moving digits to the right.

Following on from the previous step, the importance of the place holder is highlighted.

### Mathematical Talk

What is the value of each digit? Where would these digits move to if I divided the number by 10?

Which direction do I move the digits of the number when dividing by 10, 100 and 1,000?

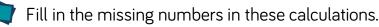
### Varied Fluency

Use the place value grid to divide 14.4 by 10, 100 and 1,000

| Т | 0 | Tths | Hths | Thths | TThth |
|---|---|------|------|-------|-------|
| • |   |      |      |       |       |

When you divide by \_\_\_\_\_, you move the counters \_\_\_\_\_ places to the right.

Fill in the missing numbers in the diagram.



$$34.2 \div = 0.342 \Rightarrow 10 = 54.1$$
  
 $\div 10 = 1.93 \div 100$ 



### Divide by 10, 100 and 1,000

### **Reasoning and Problem Solving**

